1	\$80 \$8 10 2 440 2 10 8 11 2 9 2 110 2 4 (1 11 2 2		3	M1	for continual prime factorisation (at least two correct steps anywhere) or at least two stages of a factor tree, or table, correct.  eg if first stage wrong, $800 \times 80$ then $800 = 80 \times 10$ and $80 = 40 \times 2$ would count as 2 correct steps.
				M1	dep M1 for a fully correct factor tree or a list $(2,2,2,2,5,11)$ condone inclusion of 1's on branch ends. or $2 \times 2 \times 2 \times 2 \times 5 \times 11$
		$2^4 \times 5 \times 11$		Al	dep M2 for $2^4 \times 5 \times 11$ (with working seen)
					Total 3 marks
2 (a)		2 × 3 <sup>37</sup>	1	B1	
(b)	$2 \times 3^{43} \times 2^4 \times 3^{37}$ or $2^5 \times 3^p \ (p \neq 80)$ or		2	M1	

2	(a)		$2 \times 3^{37}$	1	B1
	(b)	$2 \times 3^{43} \times 2^4 \times 3^{37}$ or $2^5 \times 3^p (p \neq 80)$ or $2^q \times 3^{80} (q \neq 5)$		2	M1
		$2^5 \times 3^p \ (p \neq 80)$ or			
		$2^q \times 3^{80} \ (q \neq 5)$			
			$2^5 \times 3^{80}$		A1
					Total 3 marks

3	(b)		2	M1	A factor tree / division ladder of 3 or
					more factors $(\neq 1)$ , multiplying to 800,
					which must include 2 and 5. Condone 1
					error when product $\neq$ 800
		$2\times2\times2\times2\times2\times5\times5$		A1	dep on M1 oe eg $2^5 \times 5^2$

4	28, 56, 84, 112 and 105, 210, 315,		2	M1for any correct valid method e.g.
	420  or 2, 2, 7 and 3, 5, 7  or $ 2 2 7 3 5 $ or $ \frac{28 \times 105}{7} \text{ or } 2, 2, 3, 5, 7 \text{ oe} $			for starting to list at least <b>four</b> multiples of each number  or 2, 2, 7 and 3, 5, 7 seen (may be in a factor tree and ignore 1)  or a fully correct Venn diagram
		420		A1 cao
				Total 2 marks

5	eg 2 × 2 × 150 or 3 × 5 × 40 or 2 × 3 × 100 or 5 <sup>2</sup> × 24 or  eg 600 2 300 2 150  eg 600 2 300 150		3	M1	for at least 2 correct stages in prime factorisation which give 2 prime factors – may be in a factor tree or a table or listed eg 2, 2, 150 (see LHS for examples of the amount of work needed for the award of this mark, allow no more than one mistake ft (eg one mistake with 2 prime factors ft: $600 = 200 \times 30 = 2 \times 100 \times 5 \times 6$ )
	eg 2 × 2 × 2 × 3 × 5 × 5     2			M1	for 2, 2, 2, 3, 5, 5 (ignore 1s) (may be a fully correct factor tree or ladder)
	Working required and note that the answer must be given as a product of powers of prime factors	$2^3 \times 3 \times 5^2$		A1	dep on M2 can be any order (allow 2 <sup>3</sup> . 3 . 5 <sup>2</sup> )
•					Total 3 marks

6	a	$2^6 \times 3 \times 11^4$	2	B2	oe, accept 2811072
				B1	for $2^a \times 3^b \times 11^c$ oe where two of $a$ , $b$ and $c$ are correct
	b	$2^9 \times 3^5 \times 11^8$	2	B2	cao
				B1	for $2^a \times 3^b \times 11^c$ oe where two of $a$ , $b$ and $c$ are correct or 2.666× $10^{13}$ or an equivalent expression for e.g. $2^2 \times 2^7 \times 3^5 \times 11^3 \times 11^5$
					Total 4 marks

7		$2^4 \times 3^2 \times 5^4 \times 11 \times 13$	2	B2	(B1 for 12 870 000 or correct unsimplified product or $2^m \times 3^n \times 5^p \times 11 \times 13$ with at least 1 of $m$ , $n$ or $p$ correct or for $2^4 \times 3^2 \times 5^4$ )
					Total 2 marks

<b>8</b> (a)		$3^2 \times 5 \times 7$ 1	B1 accep	$t \ 3 \times 3 \times 5 \times 7$ oe or $315$
9	eg 2 × 2 × 300 2 × 5 × 120 2 × 3 × 200 3 × 5 × 80 or eg  1200  1200  2 1200  3 600  200		3	M1 for at least 2 correct stages in prime factorisation which give 2 prime factors – may be in a factor tree or a table or listed eg 2, 2, 300 (allow no more than one mistake ft (eg <i>one mistake</i> with 2 prime factors ft 1200 = 20 × 600 = 2 × 10 × 3 × 200))
	2, 2, 2, 3, 5, 5 or  1200 2 600 2 200 5 100 2 20 5 10 2 20 5 10 2 2 (1)	24 2 52		M1 for finding the correct prime factors condone inclusion of 1 (may be seen in a fully correct factor tree or ladder)
		2 <sup>4</sup> ×3×5 <sup>2</sup>		A1 (dep on M2 as working requested) Can be in any order (allow 2 <sup>4</sup> . 3.5 <sup>2</sup> ) but must be in index form as asked for.
·				Total 3 marks

10 (a)	1, 2, 4, 7, 8, 14, 28, 56 and 1, 2, 3, 4, 6, 7, 12, 14, 21, 28, 42, 84 or 2 2 2 7 and 2 2 3 7 or		2	M1 for any correct valid method and no errors e.g.  for starting to list at least four different factors of each number and no errors or 2 2 2 7 and 2 2 3 7 seen (may be in a factor tree or a ladder diagram and ignore 1)  or a fully correct Venn diagram or other clear method, e.g, table
		28		A1 dep M1 accept $2^2 \times 7$ oe
(b)	60, 120, 180, 240 and 72, 144, 216, 288  or  2 2 3 5 and 2 2 2 3 3  or $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		2	M1 for any correct valid method and no errors e.g.  for starting to list at least <b>four</b> multiples of each number  or  2 2 3 5 and 2 2 2 3 3 seen  (may be in a factor tree or a ladder diagram and ignore 1)  or a fully correct Venn diagram  or other clear method, e.g, table
		360		A1 dep M1 accept $2^3 \times 3^2 \times 5$ oe
				Total 4 marks

<b>11</b> (a)	36, 72, 108, <b>and</b> 120, 240, 360,		2	M1for any correct valid method e.g.
	or			for starting to list at least three multiples of
	2, 2, 3, 3 and 2, 2, 2, 3, 5			each number
	or			
				2, 2, 3, 3 and 2, 2, 2, 3, 5 seen
				(may be in a factor tree or a ladder diagram
	$\left  \left( \begin{array}{c} 2 \\ 2 \end{array} \right) \right $			and ignore 1) (Allow $2 \times 2$ as 4)
	$\begin{pmatrix} 3 & \begin{pmatrix} 2 \\ 2 \end{pmatrix} & 25 \end{pmatrix}$			and ignore 1) (Thio ii 2 × 2 as 1)
	$\left(\begin{array}{c c} 2 & 18 & 00 \end{array}\right)$			or a fully correct "Venn" diagram
	3 9 30			of a fully correct vein diagram
	3 10			
	26,,120			
	or $\frac{36 \times 120}{12}$ or 2, 2, 2, 3, 3, 5 oe			
	12			
		360		A1 or $2^3 \times 3^2 \times 5$ oe (allow $2^3 \cdot 3^2 \cdot 5$ )
(b)		$5^2 \times 7^4 \times 11$	2	B2 for $5^2 \times 7^4 \times 11$ (in any order)
				(B1 for 660 275 or
				correct unsimplified product or
				$5^a \times 7^b \times 11^c$ where 2 of a, b and c are correct)
· · · · · · · · · · · · · · · · · · ·				Total 4 marks
				10tal 4 marks

12	2×2×7 or 2×3×7 or 3 <sup>2</sup> ×7 oe condone 1's in factor tree or showing at least 5 correct multiples across at least 2 lists (excluding 28, 42, 63) (28) 56, 84, 112, 140, 168, 196, 224, 252 (42) 84, 126, 168, 210, 252 (63) 126, 189, 252		3	M1	accept prime factors seen in factor tree or correct position in Venn diagram for at least one of the numbers given.
	$2\times2\times7$ and $2\times3\times7$ and $3\times3\times7$ or showing at least 9 correct multiples across all 3 lists (excluding 28, 42, 63)			M1	accept prime factors seen in factor tree or correct position in Venn diagram for all 3 of the numbers given.
		252		A1	or $2^2 \times 3^2 \times 7$ oe Dep on M1
12 alt	7 28 42 63 2 4 6 9 3 2 3 9 2 1 3 oe or 7 28 42 63 2 4 6 9 3 2 3 9 2 2 1 3 3 1 1 3 (1) 1 1 1		3	M1	For one correct row in table eg division by 7 gives 4, 6, 9  Fully correct table – need only go as far as top table – we want to see prime factors along the side or prime factors along the sides and bottom (condone 1's)
		252		A1	or $2^2 \times 3^2 \times 7$ oe Dep on M1
					Total 3 marks

13 (a)	2×2×2×5×5 or 2, 2, 2, 5, 5 or 2×2×3×5×7 or 2, 2, 3, 5, 7 or eg  2 200 420 2 100 210 5 50 105 10 21		2	M1	for one number written as a product of prime factors or prime factors listed – numbers may be at end of factor trees or on 'ladder diagrams' or in a table or in a Venn diagram or at least two factors for each (excluding 1, 200, 420)
	Correct answer scores full marks (unless from obvious incorrect working)	20		A1	or $2^2 \times 5$ oe
(b)	A 2 2 7 3 7 3 5 11 C		2	Ml	for $2^m \times 3^n \times 5^p \times 7^q \times 11^r$ with at least three of $m = 3$ , $n = 2$ , $p = 2$ , $q = 2$ , $r = 1$ (all 5 terms should be seen) <b>or</b> omission of one term with others fully correct <b>OR</b> prime factors seen in a Venn diagram – if so must be fully correct
	Correct answer scores full marks (unless from obvious incorrect working)	$2^3 \times 3^2 \times 5^2 \times 7^2 \times 11$		A1	allow 970 200 oe
					Total 4 marks

14	e.g. $2 \times 5 \times 225$ or $5 \times 5 \times 90$ or $5^2 \times 90$ $3 \times 5 \times 150$ or $3 \times 3 \times 250$ or $3^2 \times 250$ e.g. 2 2250 5 1125 2250 2 1125 5 225		3	M1	for 2 correct stages in prime factorisation with 0 incorrect stages or at least 3 stages in prime factorisation with no more than 1 incorrect stage. Each stage gives 2 factors – may be in a factor tree or a table or listed eg 2, 2, 225 (see LHS for examples of the amount of work needed for the award of this mark). Example of 3 stages with 1 incorrect stage: $2250 = 225 \times 100 = 3 \times 5 \times 15 \times 100$ or $225 = 3 \times 5 \times 15$
	e.g. 2 × 3 × 3 × 5 × 5 × 5  e.g. 2 2250 5 1125 3 225 5 75 3 15 5 5 5 (1) 6.g. 2250 2250 2250 2250 2250 2250 25 5 75 3 75 3 15 5 15			M1	for 2, 3, 3, 5, 5, 5 or $2 \times 3 \times 3 \times 5 \times 5 \times 5$ or $2, 3^2, 5^3$ oe or $2 + 3^2 + 5^3$ (ignore 1s) (may be a fully correct factor tree or ladder)
	Working required	$2\times3^2\times5^3$		A1	dep on M2 can be any order (allow 2 . 3 <sup>2</sup> . 5 <sup>3</sup> )

15	9, 18, 27, 36 and 12, 24, 36		4	M1 for at least two multiples of 9 and 12
	or 36			or
	or a multiple of 36			36
	or			or
	$(9 \times 12 =) 108$			a multiple of 36
	or			1
	$3^2 \times 4$ (= 36) (from Venn diagram or table)			
	"4" × 7.6(0) or "3" × 4.8(0) or			M1 for a correct method to find the cost
	"30.4" or "14.4" <b>or</b>			of 4 or 8 or 12 etc of packets of pens
	" $4n$ " × 7.6(0) or " $3n$ " × 4.8(0)			or
	411 × 7.0(0) 01 311 × 4.0(0)			3 or 6 or 9 etc packets of pencils
	"4" × 7.6(0) + "3" × 4.8(0)			M1 for a correct combination of
	or			number of packets of pens $\times$ 7.6(0) +
	"30.4" + "14.4"			number of packets of pencils $\times$ 4.8(0)
				with an intention to add
	or ((4 )) 7 ((0) + ((2 )) 4 ((0)			eg
	$"4n" \times 7.6(0) + "3n" \times 4.8(0)$			pens pencils
				$4 \times 7.60 + 3 \times 4.8 = 44.8(0)$
				$8 \times 7.60 + 6 \times 4.8 = 89.6(0)$
				$12 \times 7.60 + 9 \times 4.8 = 134.4(0)$
				$16 \times 7.60 + 12 \times 4.8 = 179.2(0)$
				$36 \times 7.60 + 27 \times 4.8 = 403.2(0)$
				$48 \times 7.60 + 36 \times 4.8 = 537.6(0)$
,	Correct answer scores full marks (unless from	44.8(0)		A1 allow 45 if 44.8(0) seen
	obvious incorrect working)			allow 4480 p or pence if £ sign crossed
				out
				M3A0 for $44.8n$ where $n$ is an integer (eg
				134.4(0))
				Total 4 marks

16 (a)	eg 2 × 2 × 75 or 3 × 5 × 20 or 2 × 3 × 50 or 5 <sup>2</sup> × 12 or  2 300 2 150 75		2	Ml	for 2 correct stages in prime factorisation with 0 incorrect stages or at least 3 stages in prime factorisation with no more than 1 incorrect stage. Each stage gives 2 factors – may be in a factor tree or a table or listed eg 2, 2, 75 (see LHS for examples of the amount of work needed for the award of this mark). Example of 3 stages with 1 incorrect stage: $300 = 100 \times 30 = 2 \times 50 \times 5 \times 6$
	Working required	$2 \times 2 \times 3 \times 5 \times 5$	1	A1	dep on M1, oe eg $2^2 \times 3 \times 5^2$
(b)	(5A =) $2 \times 2 \times 2 \times 3 \times 3 \times 5 \times 5$ oe (= 1800) or (5A =) $2^3 \times 3^2 \times 5^2$ (= 1800) or (7B =) $2 \times 2 \times 3 \times 3 \times 3 \times 5 \times 7$ oe (= 3780) or (7B =) $2^2 \times 3^3 \times 5 \times 7$ (= 3780)		2	M1	for method to find 5 <i>A</i> or 7 <i>B</i> as prime factors (may be seen in factor tree, table or Venn diagram) or as an integer  or for listing at least 3 multiples of each number eg 1800, 3600, 5400 and 3780, 7560, 11340  or for an answer of 1080 oe eg 2 <sup>3</sup> × 3 <sup>3</sup> × 5
	Working required	37800	1	A1	dep on M1, oe eg $2^3 \times 3^3 \times 5^2 \times 7$
					Total 4 marks